



2014 Indiana Academic Standards Mathematical Processes

Construct viable arguments and critique the reasoning of others.

Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They analyze situations by breaking them into cases and recognize and use counterexamples. They organize their mathematical thinking, justify their conclusions and communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and—if there is a flaw in an argument—explain what it is. They justify whether a given statement is true always, sometimes, or never. Mathematically proficient students participate and collaborate in a mathematics community. They listen to or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments.

I can *construct, justify, and communicate* arguments by...

- ◆ **considering context**
- ◆ **using examples and non-examples**
- ◆ **using objects, drawings, diagrams and actions**

I can *critique the reasoning of others* by...

- ◆ **listening**
- ◆ **comparing arguments**
- ◆ **identifying flawed logic**
- ◆ **asking questions to *clarify or improve arguments***

What to Look for:

From Students:

They understand and use prior learning in constructing arguments

From Teachers:

They provide opportunities for students to listen to or read the conclusions and arguments of others



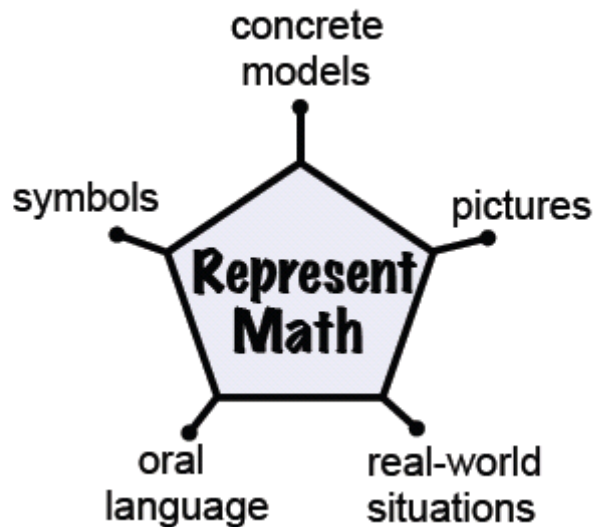
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Model with mathematics.

Mathematically proficient students apply the mathematics they know to solve problems arising in everyday life, society, and the workplace using a variety of appropriate strategies. They create and use a variety of representations to solve problems and to organize and communicate mathematical ideas. Mathematically proficient students apply what they know and are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

I can...

- ◆ **make assumptions and estimate to make complex problems easier**
- ◆ **identify important quantities and use tools to show their relationships**
- ◆ **evaluate my answer and make changes if needed**



What to Look for:

From Students: -

They analyze relationships mathematically -

From Teachers:

They provide contexts for students to apply the mathematics learned



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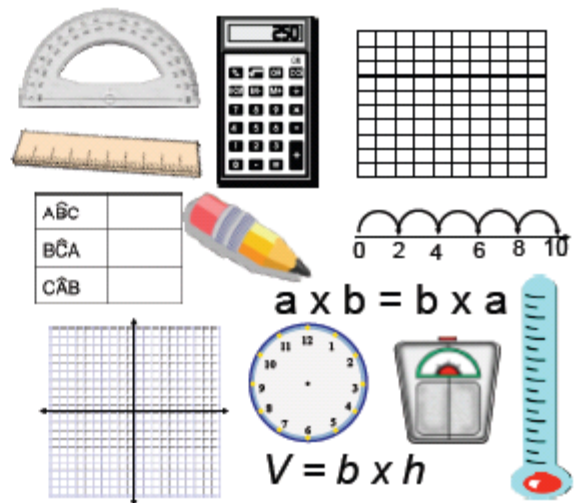
Use appropriate tools strategically.

Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Mathematically proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. Mathematically proficient students identify relevant external mathematical resources, such as digital content, and use them to pose or solve problems. They use technological tools to explore and deepen their understanding of concepts and to support the development of learning mathematics. They use technology to contribute to concept development, simulation, representation, reasoning, communication and problem solving.

I have a math toolbox.



- ◆ I know **HOW** to use math tools.
- ◆ I know **WHEN** to use math tools.
- ◆ I can reason: "Did the tool I used give me an answer that makes sense?"



What to Look for:

From Students:

They use technological tools to deepen understanding

From Teachers:

They use appropriate tools (e.g. manipulatives) instructionally



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Attend to precision. -

Mathematically proficient students communicate precisely to others. They use clear definitions, including correct mathematical language, in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They express solutions clearly and logically by using the appropriate mathematical terms and notation. They specify units of measure and label axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently and check the validity of their results in the context of the problem. They express numerical answers with a degree of precision appropriate for the problem context.

Problem Solving

- ◆ I can calculate *accurately*.
- ◆ I can calculate *efficiently*.
- ◆ My answer matches what the problem asked me to do - *estimate* or find an *exact answer*.

Communicating

- ◆ I can **SPEAK, READ, WRITE, and LISTEN** mathematically.
- ◆ I can correctly use...
 - math **symbols**
 - math **vocabulary**
 - **units of measure**

What to Look for:

From Students:

Based on a problem's expectation, students calculate with accuracy and efficiency

From Teachers:

Based on a problem's expectation, students calculate with accuracy and efficiency



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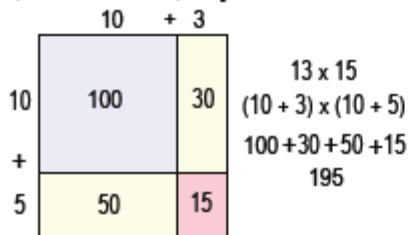
Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure. They step back for an overview and shift perspective. They recognize and use properties of operations and equality. They organize and classify geometric shapes based on their attributes. They see expressions, equations, and geometric figures as single objects or as being composed of several objects.

Numbers

For Example:

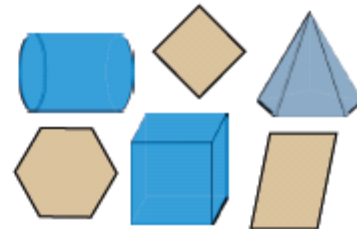
- ◆ Base 10 structure
- ◆ operations and properties
- ◆ terms, coefficients, exponents



Spaces

For Example:

- ◆ dimension
- ◆ location
- ◆ attributes
- ◆ transformation



What to Look for:

From Students: They look for patterns

From Teachers: They look for patterns



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Look for and express regularity in - repeated reasoning. -

Mathematically proficient students notice if calculations are repeated and look for general methods and shortcuts. They notice regularity in mathematical problems and their work to create a rule or formula. Mathematically proficient students maintain oversight of the process, while attending to the details as they solve a problem. They continually evaluate the reasonableness of their intermediate results.

For example: $25 \div 11$

$$\begin{array}{r} 2.\overline{27} \\ 11 \overline{)25.0000} \\ \underline{-22} \\ 30 \\ \underline{-22} \\ 80 \\ \underline{-77} \\ 30 \\ \underline{-22} \\ 80 \\ \underline{-77} \\ 30 \end{array}$$

I am repeating this calculation. The quotient is a repeating decimal.

What to Look for:

From Students:

They regularly check the reasonableness of their results

From Teachers:

They encourage students to look for and discuss regularity in reasoning