



This Teacher Resource Guide, revised in July 2018, provides supporting materials to help educators successfully implement the Indiana Academic Standards for Algebra 2. This resource guide is provided to help ensure all students meet the rigorous learning expectations set by the academic standards. Use of this guide and the resources on the web page is optional – teachers should decide which resources will work best for their students. However, all guidance contained in this document and on the website has been chosen to best support effective teaching practices and promote the Mathematics Process Standards.

With an increased emphasis on content area literacy, academic vocabulary has been noted. Best practices should be utilized when teaching students academic vocabulary. Please see the Literacy Framework and the Science and Technical Subjects Content Area Literacy Standards for examples of best practices.

Examples have been removed from the document as they tend to limit interpretation and classroom application. Rather, success criteria, in the form of "I can" statements, have been included. According to Hattie (2017), success criteria is specific, concrete and measurable, describing what success looks like when a learning goal is reached. Additionally, success criteria contributes to teacher clarity, which has a 0.75 effect size! An effect size of 0.40 reportedly indicates one year of growth. Utilizing success criteria in the classroom allows students to monitor their own learning and increases motivation (Hattie, p. 57). It is important to note that the success criteria provided here are not intended to be limiting. Teachers may have additional success criteria for their students.

Guidance around vertical articulation has been provided in the last two columns. Knowing what was expected of students at previous grade levels will help teachers connect new learning to prior knowledge. Additionally, understanding what a student will be expected to learn in the future provides the teacher a context for the current learning. This information is not exhaustive; rather it is provided to give teachers a quick understanding of how the work builds from previous grade levels into subsequent courses. The Indiana Department of Education (IDOE) math team recommends teachers further study this vertical articulation to situate their course objectives in the broader math context.

If you have any questions, please do not hesitate to reach out to the IDOE math team. Contact information for the Elementary and Secondary Math Specialists can be found on the website: <a href="https://www.doe.in.gov/standards/mathematics">https://www.doe.in.gov/standards/mathematics</a>. If you have suggested resources for the website, please share those as well.

Hattie, J., Fisher, D., Frey, N., Gojak, L. M., Moore, S. D., & Mellman, W. (2017). *Visible learning for mathematics: What works best to optimize student learning, grades K-12*. Thousand Oaks, CA: Corwin Mathematics.





	Complex Numbers and Expressions					
Algebra 2 Ma	athematics Standards	Success Criteria	Academic Vocabulary	Looking Back	Looking Ahead	
MA.AII.CNE.1:	Know there is an imaginary number, $i$ , such that $i^2 = -1$ , and every complex number can be written in the form $a + bi$ , with $a$ and $b$ real. Use the relation $i^2 = -1$ and the commutative, associative, and distributive properties to add, subtract, and multiply complex numbers.	I can understand the idea of the imaginary number, <i>i</i> , as being the square root of negative one.  I can use the relation <i>i</i> <sup>2</sup> = -1 to simplify expressions.  I can identify the real and the imaginary parts of complex numbers written in the form <i>a</i> + <i>bi</i> .  I can add, subtract, and multiply complex numbers.  I can recognize that the commutative, associative, and distributive properties extend to the set of complex numbers over the operations of addition and multiplication.	Complex number	Understand the hierarchy and relationships of numbers within the real number system. (MA.AI.RNE.1)	Calculate the distance and midpoint between numbers in the complex plane. (MA.PC.PCN.1)  Understand and use complex numbers, including real and imaginary numbers. (MA.PC.PCN.2)  Understand and use addition, subtraction, multiplication, and conjugation of complex numbers. (MA.PC.PCN.3)	
MA.AII.CNE.2:	Translate expressions between radical and exponent form and simplify them using the laws of exponents.	I can translate expressions between radical and exponent form.	Radical expression  Exponential expression	Rewrite and evaluate numeric expressions with positive rational exponents using the properties of		





		I can simplify expressions written in exponent form with rational exponents using the laws of exponents.	Product of powers  Quotient of powers  Power of a power  Power of a product  Power of a quotient	exponents. (MA.AI.RNE.3)	
MA.AII.CNE.3:	Understand that rational expressions form a system analogous to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression; add, subtract, multiply, and divide algebraic rational expressions.	I can explore operations with rational expressions to determine whether they are closed under addition, subtraction, multiplication, and division by a nonzero rational expression.  I can connect my understanding of rational expressions to my understanding of rational numbers.  I can add and subtract rational expressions with common denominators.  I can add and subtract rational expressions without common	Rational expression Rational numbers	Explain why the sum or product of two rational numbers is rational; that the sum of a rational number and an irrational number is irrational; and that the product of a nonzero rational number and an irrational number is irrational number is irrational. (MA.AI.RNE.2)  Understand polynomials are closed under the operations of addition, subtraction, and multiplication with integers. (MA.AI.RNE. 7)	





		denominators by finding the common denominator.			
		I can multiply and divide rational expressions.			
MA.AII.CNE.4:	Rewrite algebraic rational expressions in equivalent forms (e.g., using laws of exponents and factoring techniques).	I can rewrite algebraic expressions in equivalent forms using the laws of exponents.  I can rewrite algebraic expressions in equivalent forms using factoring	Product of powers  Quotient of powers  Power of a power	Simplify algebraic rational expressions, with numerators and denominators containing monomial bases with integer exponents. (MA.AI.RNE.5)	
		techniques.	Power of a product Power of a quotient Factoring	Factor common terms from polynomials and factor polynomials completely. Factor the difference of two squares, perfect square trinomials, and other quadratic expressions.  (MA.AI.RNE.6)	
MA.AII.CNE.5:	Rewrite rational expressions in different forms; write a(x)/b(x) in the form q(x) + r(x)/b(x), where a(x), b(x), q(x), and r(x) are polynomials with the degree of r(x) less than the degree	I can rewrite rational expressions using long division.  I can identify the degree of a polynomials.	Rational expression Polynomials Degree Synthetic division	Simplify algebraic rational expressions, with numerators and denominators containing monomial bases. (MA.AI.RNE.5)	Know and apply the Remainder Theorem. (MA.PC.QPR.3)  Understand the Fundamental Theorem of Algebra; find a polynomial function of lowest





	of b(x), using long division and synthetic division.	I can rewrite rational expressions using synthetic division.  I can identify the divisor to use in order to perform synthetic division.	Polynomial long division		degree with real coefficients when given its roots. (MA.PC.QPR.4)
MA.AII.CNE.6:	Find partial sums of arithmetic and geometric series and represent them using sigma notation.	I can find partial sums of arithmetic series.  I can find partial sums of geometric series.  I can represent partial sums of arithmetic and geometric series using sigma notation.  I can understand the parts of a series written in sigma notation.	Partial sum Arithmetic series Geometric series Sigma notation	Represent linear functions as graphs from equations (with and without technology), equations from graphs, and equations from tables and other given information. (MA.AI.L.4)  Represent real-world problems that can be modeled with a linear function. (MA.AI.L.5)  Distinguish between situations that can be modeled with linear functions and with exponential functions.  Understand that linear functions grow by equal differences over equal intervals,	Model and solve real-world problems involving applications of sequences and series and interpret the solutions. (MA.PC.F.8)  Recognize an infinite series as the limit of a sequence of partial sums. (MA.PC.F.10)





	and that exponential functions grow by equal factors over equal intervals. (MA.AI.QE.1)
	Represent real-world and other mathematical problems that can be modeled with
	exponential functions using tables, graphs, and equations. (MA.AI.QE.2)

Functions						
Algebra 2	Mathematics Standards	Success Criteria	Academic Vocabulary	Looking Back	Looking Ahead	
MA.AII.F.1:	Determine whether a relation represented by a table, graph, or equation is a function.	I can determine whether a relation is a function given a table.  I can determine whether a relation is a function given a graph.  I can determine whether a relation is a function given an equation.	Relation	Understand that a function from one set to another set assigns to each element of the domain exactly one element of the range. (MA.AI.F.1)		





MA.AII.F.2:	Understand composition of functions and combine functions by composition.	I can combine functions by substituting one function in for the other.  I can understand and explain the process of composing functions.	Composition of functions	Solve pairs of linear equations in two variables using substitution. (MA.AI.SEI.2)	
MA.AII.F.3:	Understand that an inverse function can be obtained by expressing the dependent variable of one function as the independent variable of another, as f and g are inverse functions if and only if f(x)=y and g(y)=x, for all values of x in the domain of f and all values of y in the domain of g. Find the inverse of a function that has an inverse.	I can understand that the inverse of a function is obtained by switching the dependent and independent variables then isolating the dependent variable.  I can understand the idea that the inverse of a function "undoes" anything the original function does.  I can determine whether a function has an inverse.  I can determine if a function is one-to-one.  I can use the horizontal line test to determine whether the graph of a function has an inverse.	Inverse function  Dependent variable  Independent variable  Domain  Horizontal line test  One-to-one	Understand that if f is a function and x is an element of its domain, then f(x) denotes the output of f corresponding to the input of x. (MA.AI.F.1)  Solve equation and formulas for a specified variable. (MA.AI.L.11)	Determine if a graph or table has an inverse, and justify if the inverse is a function, relation, or neither.(MA.PC.F.4)  Produce an invertible function from a non-invertible function by restricting the domain. (MA.PC.F.5)





MA.AII.F.4:	Understand that if the graph of a function contains a point (a, b), then the graph of the inverse relation of the function contains the point (b, a); the inverse is a reflection over the line	I can understand the domain of a function is the range of the inverse, and vice versa.  I can graph a function and its inverse to show that the inverse is a reflection of the function over the line y= x.	Reflection Inverse relationship	Identify the domain and range of relations in tables and graphs. (MA.AI.F.3)	Identify the values of an inverse function/relation from a graph or table. (MA.PC.F.4)
MA.AII.F.5:	Describe the effect on the graph of f(x) by replacing f(x) with f(x) + k, k f(x), f(kx), and f(x + k) for specific values of k (both positive and negative) with and without technology. Find the value of k given the graph of f(x) and the graph of f(x) + k, k f(x), f(kx), or f(x + k).	I can identify the transformations of a function on a graph.  I can describe the effects of transformations on parent functions.  I can determine the value corresponding to various transformations of functions.	Parent function  Transformation	Describe qualitatively the functional relationship between two quantities by analyzing a graph. (MA.AI.F.2)	Describe the effect on the graph of f(x) by replacing f(x) with f(x) + k, k f(x), f(kx), and f(x + k) for specific values of k. (MA.PC.F.6)  Determine how the graph of a parabola changes if a, b, and c changes in the equation y = a(x-b) <sup>2</sup> +c. (MA.TR.CO.1)

Systems of Equations						
Systems of Equations						
Algebra 2 Mathematics Standards	Success Criteria	Academic Vocabulary	Looking Back	Looking Ahead		





MA.AII.SE.1:	Solve a system of equations consisting of a linear equation and a quadratic equation in two variables algebraically and graphically with and without technology (e.g., find the points of	I can solve a system of equations consisting of linear and quadratic equations in two variables algebraically.  I can solve a system of equations consisting of linear and quadratic equations in two	System of equations  Linear equation  Quadratic equation  Point of intersection	Solve pairs of linear equations in two variables using substitution and elimination. (MA.AI.SEI.2)	
	intersection between the line $y = -3x$ and the circle $x^2 + y^2 = 3$ .	variables graphically by finding the point(s)s of intersection with and without technology.			
MA.AII.SE.2:	Solve systems of two or three linear equations in two or three variables algebraically and using technology.	I can solve a system of two or three linear equations in two or three variables algebraically.  I can solve a system of two or three linear equations in two or three variables using technology.	System of equations  Composition  Elimination method  Substitution method	Solve pairs of linear equations in two variables using substitution and elimination. (MA.AI.SEI.2)  Solve systems of two linear equations in two variables with and without technology.	
MA.AII.SE.3:	Represent real-world problems using a system of linear equations in three variables and solve such problems with and without technology. Interpret the solution and	I can represent real-world problems using a system of linear equation in three variables.  I can solve real-world problems using a system of	System of equations Inverse function Dependent variable Independent variable	(MA.AI.SEI.3)  Represent and solve real-world problems using a system of two linear equation in two variables; interpret the solution and determine whether it is	





determine whether it is reasonable.	linear equations in three variables.	Domain	reasonable. (MA.Al.SEI.3)	
	I can interpret the solution to a system of linear equations in three variables and determine whether it is reasonable.			

	Quadratic Equations and Functions						
Algebra 2 N	Mathematics Standards	Success Criteria	Academic Vocabulary	Looking Back	Looking Ahead		
MA.AII.Q.1:	Represent real-world problems that can be modeled with quadratic functions using tables, graphs, and equations; translate fluently among these representations. Solve such problems with and without technology. Interpret the solutions and determine whether they are reasonable.	I can represent and solve real-world problems that can be modeled with quadratic functions using a table.  I can represent and solve real-world problems that can be modeled with quadratic functions using a graph.  I can represent and solve real-world problems that can be modeled with quadratic functions using an equation.	Quadratic function	Represent real-world problems using quadratic equations in one or two variables and solve with and without technology; interpret the solution and determine whether it is reasonable. (MA.AI.QE.5)			





		I can translate fluently among tables, graphs, and equations of quadratic functions.  I can interpret my solution to a quadratic function and determine its reasonableness.			
MA.AII.Q.2:	Use completing the square to rewrite quadratic functions into the form $y = a(x + h)^2 + k$ , and graph these functions with and without technology. Identify intercepts, zeros, domain and range, and lines of symmetry. Understand the relationship between completing the square and the quadratic formula.	I can use the technique of completing the square to rewrite quadratic functions into the form y = a(x + h) <sup>2</sup> + k.  I can graph quadratic functions in the from y = a(x + h) <sup>2</sup> + k with and without technology.  I can identify important features of quadratic function, including intercepts, zeros, domain and range, and line of symmetry.  I can understand the relationship between completing the square and the quadratic formula.	Completing the square  Quadratic function  Vertex form of a quadratic equation  Intercepts  Zeros  Domain  Range  Line of symmetry  Quadratic formula	Solve quadratic equations in one variable using the quadratic formula. (MA.AI.QE.4)  Use the process of factoring to determine zeros, lines of symmetry and extreme values. (MA.AI.QE.6)  Describe the relationship among solutions of a quadratic, the zeros, the x-intercepts, and the factors. (MA.AI.AE.7)	Use the method of completing the square to transform any quadratic equation of the form $(x - p)^2 = q$ ; derive the quadratic formula from this form. (MA.PC.QPR.1)  Complete the square to find the center and radius of a circle given by an equation. (MA.TR.CO.3)
MA.AII.Q.3:	Use the discriminant to determine the number and type of solutions of a quadratic equation in one	I can identify the discriminant within the quadratic formula.	Discriminant  Quadratic formula	Solve quadratic equations in one variable using the quadratic formula. (MA.AI.QE.4)	





variable with real coefficients; find all solutions and write complex solutions in form of a ± bi for real numbers a and b.		Quadratic equation  Complex solutions	Describe the relationship among solutions of a quadratic, the zeros, the x-intercepts, and the factors. (MA.AI.AE.7)	
	I can write complex solutions in the form $a \pm bi$ .			

	Exponential & Logarithmic Equations and Functions						
Algebra 2 N	lathematics Standards	Success Criteria	Academic Vocabulary	Looking Back	Looking Ahead		
MA.AII.EL.1:	Write arithmetic and geometric sequences both recursively and with an explicit formula; use them to model situations and translate between the two forms.	I can write an arithmetic sequences both recursively and explicitly.  I can write a geometric sequence both recursively and explicitly.  I can use arithmetic and geometric sequences to model situations.	Arithmetic sequence Geometric sequence Recursive formula Explicit formula	Understand that linear functions grow by equal differences over equal intervals and the exponential functions grow by equal factors over equal intervals. (MA.AI.QE.1)	Recognize that sequences are functions, sometimes defined recursively. (MA.PC.F.3)  Define arithmetic and geometric sequences recursively; model and solve real-world problems involving applications of sequences and		





		I can translate between recursive formulas and explicit formulas.			series and interpret the solutions. (MA.PC.F.8)  Decide whether simple sequences converge or diverge. (MA.PC.F.10)
MA.AII.EL.2:	Graph exponential functions with and without technology. Identify and describe features, such as intercepts, zeros, domain and range, and asymptotic and end behavior.	I can graph exponential functions with and without technology.  I can identify and describe important features of exponential functions such as intercepts, zeros, domain and range, and asymptotic and end behavior.	Exponential function Asymptote End behavior Intercepts Zeros Domain Range	Graph exponential equations in two variables with and without technology. (MA.QE.3)  Describe qualitatively the functional relationship between two quantities by analyzing a graph. (MA.AI.F.2)	Graph rational functions with and without technology; identify and describe features, such as intercepts, domain and range, and asymptotic and end behavior.  (MA.PC.QPR.2)
			Initial value		
MA.AII.EL.3:	Identify the percent rate of change in exponential functions written as equations, such as y = (1.02)^t, y = (0.97)^t, y = (1.01)12^t, y = (1.2)^t/10, and classify them as	I can identify the percent rate of change in an exponential function.  I can classify an exponential function as representing growth or decay based upon the percent rate of change.	Percent rate of change  Exponential growth  Exponential decay	Represent real-world and other mathematical problems that can be modeled with exponential functions using tables, graphs, and equations. (MA.AI.QE.2)	





	representing exponential				
	growth or decay.	I can distinguish between the			
		growth or decay rate and the			
		factor by which something			
		grows or decays.			
MA.AII.EL.4:	Use the properties of	I can use the properties of	Properties of	Rewrite numeric	
	exponents to transform	exponents to transform	exponents	expressions using	
	expressions for	expressions for exponential		the properties of exponents.	
	exponential functions	functions.	Exponential function	(MA.AI.RNE.3)	
	(e.g., the expression			(WALS U.I CIVE.O)	
	1.15 <sup>t</sup> can be rewritten	I can find equivalent monthly			
	as (1.15^1/12)^12t ≈	interest rate given annual			
	1.012^12t to reveal the	interest rates.			
	approximate equivalent				
	monthly interest rate if				
	the annual rate is 15%).				
MA.AII.EL.5:	Know that the inverse of	I can identify and justify the	Inverse		
	an exponential function	logarithmic function as the			
	is a logarithmic function.	inverse of an exponential	Exponential function		
	Represent exponential	function.			
	and logarithmic functions		Logarithmic function		
	using graphing	I can graph exponential			
	technology and describe	functions using technology.	Inverse relationship		
	their inverse relationship.				
		I can graph logarithmic			
		functions using technology.			
		I can describe the inverse			
		relationship of exponential and			
		logarithmic functions.			





MA.AII.EL.6:	Use the laws of	I can use the laws of	Laws of exponents		Convert logarithms
	exponents to derive the	exponents to derive the laws			from one base to
	laws of logarithms. Use	of logarithms.	Laws of logarithms	-	another and prove
	the laws of logarithms		, and the second		simple laws of
	and the inverse	I can use the laws of	Inverse relationship		logarithms.
	relationship between	logarithms to evaluate	р		(MA.PC.EL.1)
	exponential functions	expressions and solve	Exponential		Use the laws of
	and logarithms to	equations in one variable.	functions		logarithms to simplify
	evaluate expressions	equations in one variable.	TUTICUOTIS		logarithmic
	and solve equations in	I can understand the inverse	Logarithm		expressions and find
	one variable.		Logantiiii		their approximate
	one variable.	relationship between			values.
		exponential functions and			(MA.PC.EL.2)
		logarithms.			
MA.AII.EL.7:	Represent real-world	I can represent and solve real-	Exponential	Represent real-world and other	Graph and solve real-world and other
	problems using	world problems using	equation	mathematical	mathematical
	exponential equations in	exponential equations in one		problems that can be	problems that can be
	one or two variables and	variable.		modeled with	modeled using
	solve such problems with			exponential functions	exponential and
	and without technology.	I can represent and solve real-		using tables, graphs,	logarithmic equations
	Interpret the solutions	world problems using		and equations.	and inequalities.
	and determine whether	exponential equations in two		(MA.AI.QE.2)	(MA.PC.EL.3)
	they are reasonable.	variables.			
		I can interpret my solution to			
		an exponential equation and			
		determine the reasonableness			
		of it.			





Polynomial, Rational, and Other Equations and Functions						
Algebra 2 M	lathematics Standards	Success Criteria	Academic Vocabulary	Looking Back	Looking Ahead	
MA.AII.PR.1:	Solve real-world and other mathematical problems involving polynomial equations with and without technology. Interpret the solutions and determine whether the solutions are reasonable.	I can solve real-world problems involving polynomial equations.  I can solve mathematical problems involving polynomial equations.  I can interpret the solution to a polynomial equation and determine the reasonableness of it.	Polynomial equation	Factor polynomials completely. (MA.AI.RNE.6)  Add, subtract, and multiply polynomials and divide polynomials by monomials. (MA.AI.RNE.7)		
MA.AII.PR.2:	Graph relations and functions including polynomial, square root, and piecewise-defined functions (including step functions and absolute value functions) with and without technology. Identify and describe features, such as intercepts, zeros, domain and range, end behavior, and lines of symmetry.	I can graph polynomial functions.  I can graph square root functions.  I can graph piece-wise defined functions, including step functions and absolute value functions.  I can graph relations and functions and identify and describe important features such as intercepts, zeros,	Relation Function Polynomial function Square-root function Piecewise function Step function Absolute-value function	Graph absolute value linear equation in two variables. (MA.AI.L.10)  Graph exponential and quadratic equations in two variables. (MA.AI.QE.3)  Describe qualitatively the functional relationship between two quantities by analyzing a graph. (MA.AI.F.2)	Interpret key features of graphs and tables in terms of quantities and sketch showing key features given verbally; key features include intercepts, intervals of increase and decrease, intervals where function is positive and negative, relative maximums/minimum, end behavior, periodicity. (MA.PC.F.1)	





		domain and range, end behavior, and lines of symmetry.	Intercepts Zeros	
			Domain	
			Range	
			End behavior	
			Line of symmetry	
			Asymptote	
MA.AII.PR.3:	Solve real-world and other mathematical	I can solve real-world problems involving rational	Rational function	
	problems involving rational and radical	functions.	Radical function	
	functions, including direct, inverse, and joint	I can solve real-world problems involving radical	Direct variation	
	variation. Give examples showing how extraneous	functions.	Inverse variation	
	solutions may arise.	I can solve mathematical problems involving rational	Joint variation	
		functions.	Extraneous solution	
		I can solve mathematical		
		problems involving radical		
		functions.		





I can solve real-world and	
mathematical problems	
involving direct variation	
functions.	
I can solve real-world and	
mathematical problems	
involving inverse variation	
functions.	
I can solve real-world and	
mathematical problems	
involving joint variation	
functions.	
I can identify and understand	
extraneous solutions and	
situations in which they may	
arise.	

Data Analysis, Statistics, and Probability							
Algebra 2 Mathematics Standards		Success Criteria	Academic Vocabulary	Looking Back	Looking Ahead		
MA.AII.DSP.1	Make inferences and justify conclusions from sample surveys, experiments, and observational studies.	I can make inferences from sample surveys, experiments, and observational studies.	Inference Sample survey Experiments	Evaluate the characteristics of a good survey and well-designed experiment, design	Identify limitations, strengths, or lack of information in studies, including data collection		





	Recognize the purposes of and differences among sample surveys, experiments, and observational studies; explain how randomization relates to each.	I can justify my conclusions made from inferences based off of sample surveys, experiments, and observational studies.  I can recognize the differences among sample surveys, experiments, and observational studies.  I can explain how randomization relates to sample surveys, experiments, and observational studies.	Observational study Randomization	simple experiments or investigations to collect data to answer questions of interest, and make inferences from sample results. (MA.AI.DS.1)  Understand that statistics and data are non-neutral and designed to serve a particular interest. (MA.AI.DS.6)	methods (e.g. sampling, experimental, observational) and possible sources of bias. (MA.QR.S.2)
MA.AII.DSP.2	Use technology to find a linear, quadratic, or exponential function that models a relationship for a bivariate data set to make predictions; compute (using technology) and interpret the correlation coefficient.	I can use technology to fit a linear, quadratic, or exponential model to a relationship for a bivariate data set.  I can make predictions using an appropriate model for a bivariate data set.  I can use technology to compute the correlation coefficient.	Bivariate data  Correlation coefficient  Linear function  Quadratic function  Exponential function	Use technology to find a linear function that models a relationship for a bivariate data set to make predictions; compute (using technology) and interpret the correlation coefficient. (MA.AI.DS.3)	Use technology to find a quadratic, exponential, logarithmic, or power function that models a relationship for a bivariate data set to make predictions. (MA.PC.EL.4)  Analyze and critique mathematical models and be able to describe their limitations, including distinguishing between correlation





		I can interpret the correlation coefficient of an appropriate model for a bivariate data set.			and causation. (MA.QR.M.1) Choose and create
					linear, exponential, logistic, or periodic models and curves of best fit for bivariate data sets; use the models to answer questions and draw conclusions or make decisions, addressing limitations and long-term ramifications of chosen models.
MA.AII.DSP.3	Organize, graph (e.g.,	I can organize and graph	Box-and -whisker	Make observations	(MA.QR.M.3) Read, interpret, and
:	line plots and box plots),	univariate data using line plots	plot	about the degree of visual overlap of two	make decisions about data
	and compare univariate data of two or more different data sets using	and box plots.  I can compare univariate data	Univariate data	numerical data distributions	summarized numerically using
	measures of center	of two or more different data	Interquartile range	represented in line plots or box plots.	measures of center and spread, in
	(mean and median) and	sets using measures of center,	(IQR)	(MA.7.DSP.4)	tables, and in
	spread (range, interquartile range, standard deviation, percentiles,	including median and mean).  I can compare univariate data	Standard deviation	Describe how outliers affect the	graphical displays (line graphs, bar graphs, scatterplots,
	and variance). Understand the effects of	using measures of spread, including range, interquartile	Variance	mean and/or median. (MA.7.DSP.4)	and histograms). (MA.QR.S.5)
			Percentile	Find, use, and interpret measures of	Compare center, shape, and spread of





	outliers on the statistical summary of the data.	range, standard deviation, percentiles, and variance.  I can identify and understand the effects of outliers on the statistical summary of univariate data.	Outlier  Mean  Median  Range	center and measures of spread for numerical data. (MA.7.DSP.3)	two or more data sets and interpret the differences in context. (MA.QR.S.7)
MA.AII.DSP.4	Record multiple observations (or simulated samples) of random events and construct empirical models of the probability distributions. Construct a theoretical model and apply the law of large numbers to show the relationship between the two models.	I can record multiple observations of random events.  I can construct empirical models of probability distributions.  I can construct a theoretical model.  I can apply the law of large numbers.  I can explain the relationship between a theoretical model and the empirical model.	Simulation  Empirical model  Theoretical model  Law of large numbers	Develop probability models; compare probabilities from the model to observed frequencies. (MA.7.DSP.7)	Evaluate the validity of claims based on empirical, theoretical, and subjective probabilities. (MA.QR.P.3)
MA.AII.DSP.5	Understand dependent and independent events, and conditional probability; apply these	I can distinguish between dependent, independent events and conditional probability.	Conditional probability  Dependent event	Understand and use terminology to describe independent and dependent events. (MA.8.DSP.4)	Use data displays and models to determine probabilities (including conditional





	concepts to calculate probabilities.	I can apply properties of dependent events and independent events to calculate probabilities.	Independent event	Find probabilities of compound events (independent and dependent). (MA.8.DSP.5)	probabilities). (MA.QR.P.4)
MA.AII.DSP.6	Understand the multiplication counting principle, permutations, and combinations; apply these concepts to calculate probabilities.	I can understand the multiplication counting principle.  I can distinguish between a permutation and a combination.  I can apply the properties of permutations and combinations to calculate probabilities.  I can understand the necessity for and use of factorial notation.  I can use factorial notation when calculating permutations and combinations.	Permutation Combination Factorial	For events with a large number of outcomes, understand the use of and apply the multiplication counting principle. (MA.8.DSP.6)	